



**UNCONVENTIONAL RESERVOIR ENGINEERING PROJECT**  
Colorado School of Mines



## Research Summary

Molecular Modeling of Filtration in Nanoporous Media

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# Objectives

- Explain the concept of selective permeability
- Predict the movement of the molecules across the membrane based on their composition
- Interpret and graph kinetics of molecule transport across the semi-permeable membrane



# Semi-permeable membrane allows

- Only small molecules to cross.
- Only charged molecules to cross.
- Certain molecules to enter the membrane but not cross to the other side.
- Molecules to cross the membrane until they reach equal concentration on both sides.
- Molecules to cross dependent upon their chemical characteristics.



# Diffusion

“The movement of particles in a solid from an area of **high** concentration to an area of **low** concentration resulting in the uniform distribution of the substance”

- During diffusion molecules move down a concentration gradient

$$J = -D \frac{dC}{dx}$$

*D*- diffusion coefficient



# Diffusion Coefficient

- Diffusion coefficient increases with increasing temperature (T)

$$D = \rho_g d_p \left( \frac{8RT}{\pi M} \right)^{\frac{1}{2}} e^{-\frac{\Delta E}{RT}}$$

$D$  = diffusion coefficient [m<sup>2</sup>/s]

$D_o$  = pre-exponential [m<sup>2</sup>/s]

$Q_d$  = activation energy [J/mol or eV/atom]

$R$  = gas constant [8.314 J/mol-K]

$T$  = absolute temperature [K]



# Permeability coefficient

$$P = D_{c,ads} * \left( \frac{d \ln(p)}{d \ln(C_{ads})} \right) \left( \frac{\theta}{\tau} \right) \frac{dC_{ads}}{dp} + \frac{\theta}{\tau} \frac{D_{c,gas}}{RT}$$

$$D_{c,ads} = \rho_g d_p \left( \frac{8RT}{\pi M} \right)^{\frac{1}{2}} e^{-\frac{E_{ads}}{RT}}$$

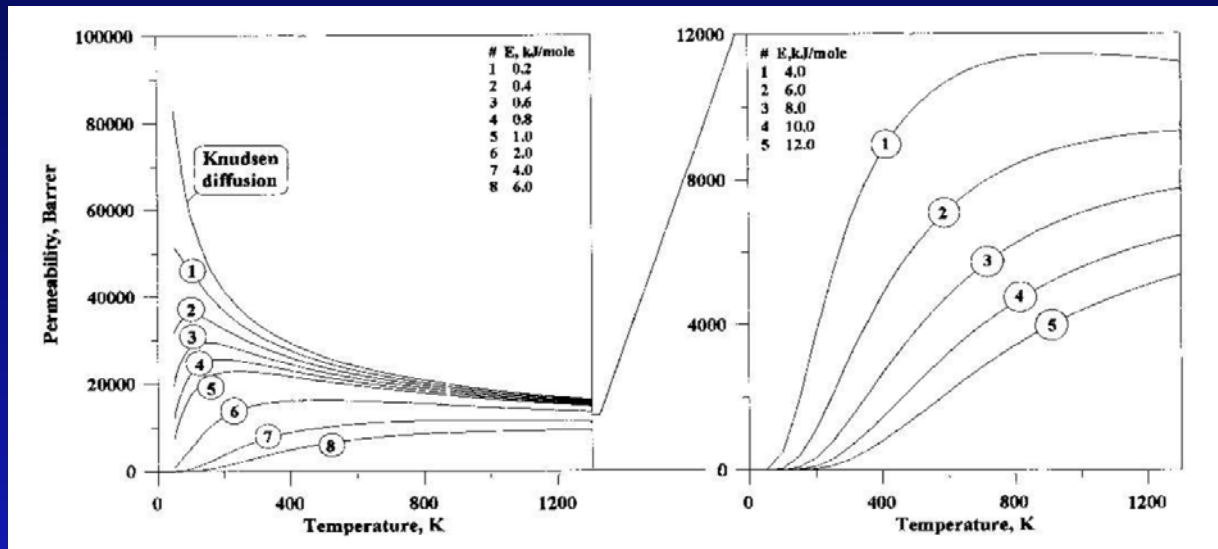
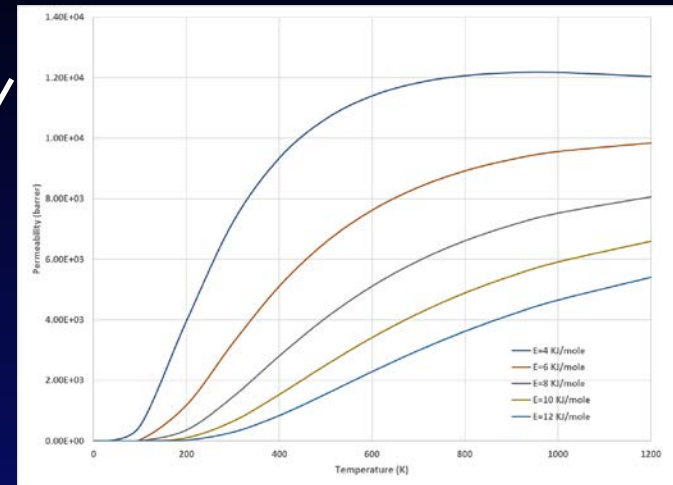
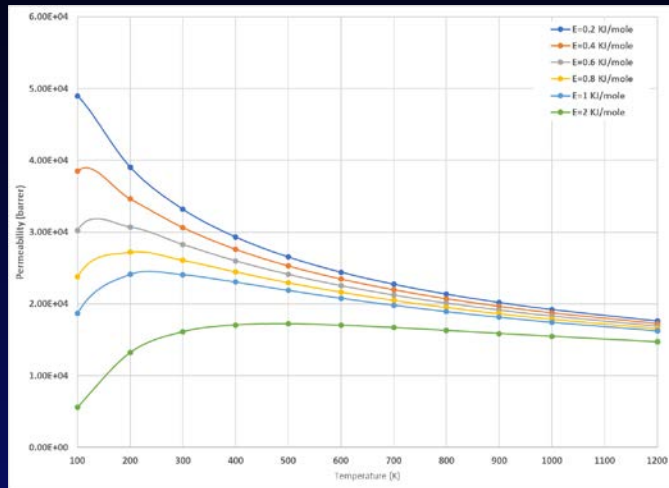
$$D_{c,gas} = \rho_g d_p \left( \frac{8RT}{\pi M} \right)^{\frac{1}{2}} e^{-\frac{E_{gas}}{RT}}$$

For permanent gases:

$$P = \rho_g d_p \left( \frac{8}{\pi RTM} \right)^{\frac{1}{2}} \frac{\theta}{\tau} e^{-\frac{E_{gas}}{RT}}$$



# Upper bound of permeability coefficient




Shelekhin et al., 1995



# Selectivity of gas separation

- Selectivity factor is defined as the ratio of the permeability coefficients
- Only exponential term depends on temperature

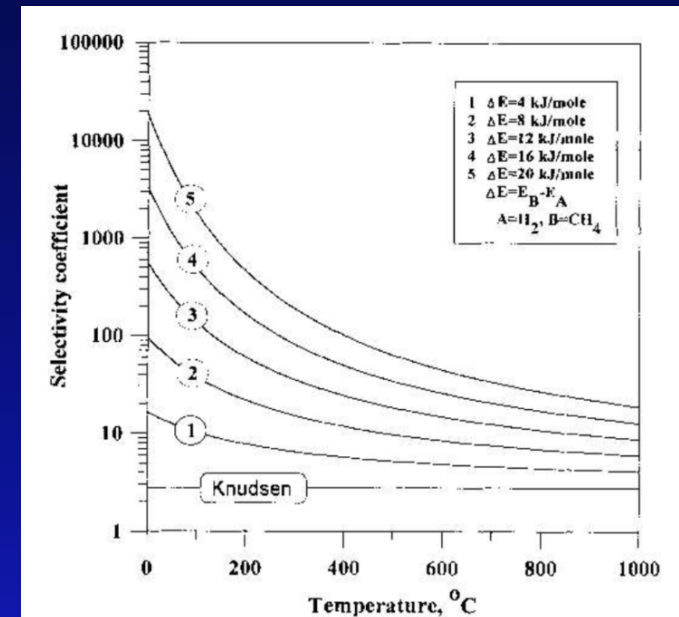
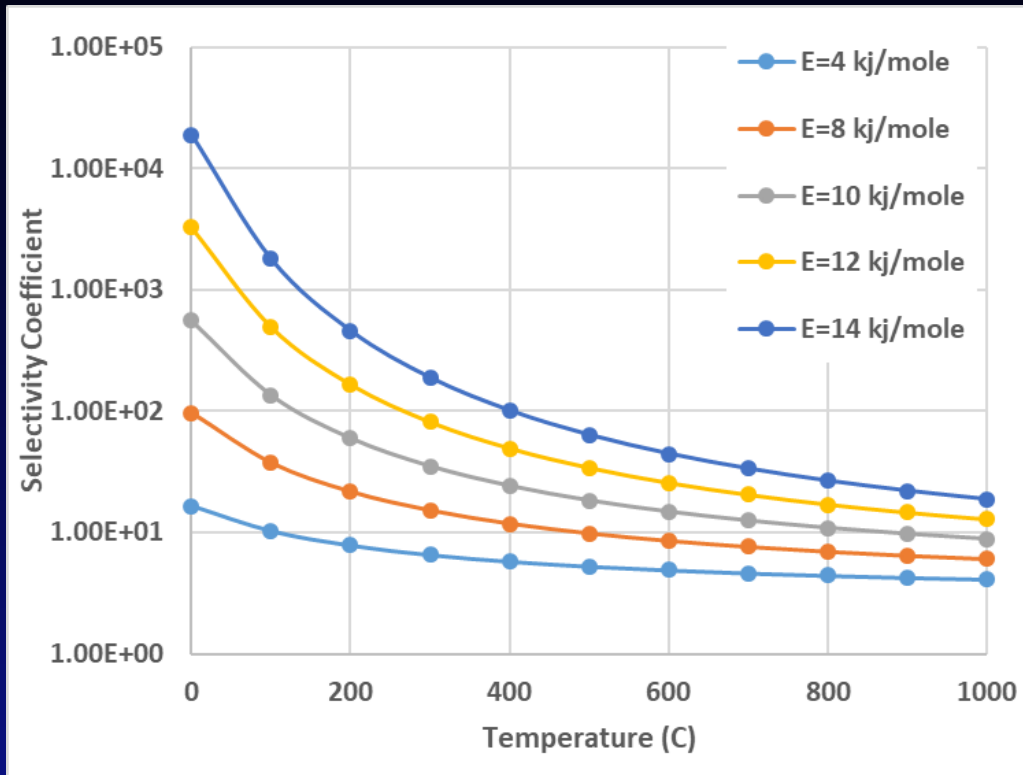
$$\alpha = \frac{P_a}{P_b} = \left( \frac{M_B}{M_A} \right)^{\frac{1}{2}} \exp\left( -\frac{\Delta E_A - \Delta E_B}{RT} \right)$$


Shelekhin et al., 1995





# Selectivity of gas separation



Shelekhin et al., 1995



**UNCONVENTIONAL RESERVOIR ENGINEERING PROJECT**

Advisory Board Meeting, November 9, 2018, Golden, Colorado

# Future Works

- Determine the dependence of permeability coefficients on temperature
- Determine the dependency of activation energy of diffusion and pore size kinetic diameter
- Create a theoretical model of gas permeation in microporous molecular-sieve membranes

Shelekhin et al., 1995



Thank you!  
Question?

