



**UNCONVENTIONAL RESERVOIR ENGINEERING PROJECT**  
Colorado School of Mines



## **Research Summary**

# **Transient Drainage Volume of Fractured Horizontal Wells**

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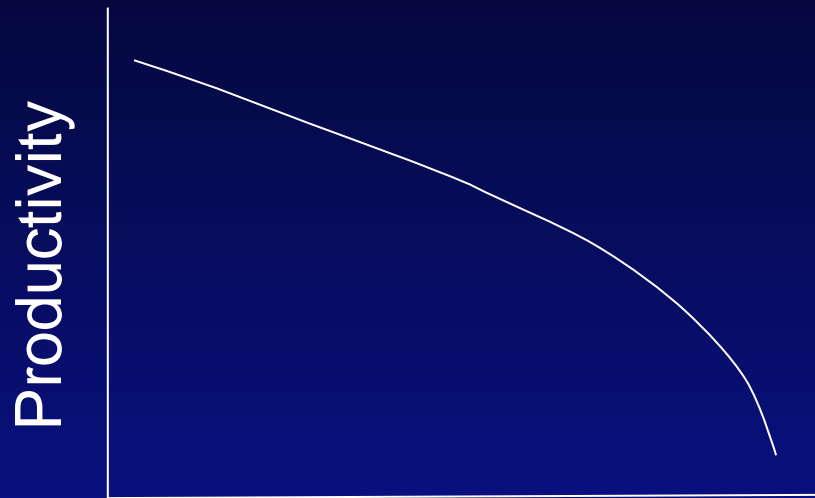
# Outline

- **Conventional Wisdom of Well Spacing**
- **Unconventional Wells**
- **Well Spacing Problem for Unconventional Projects**
- **Transient Drainage Area**
- **Conclusions**

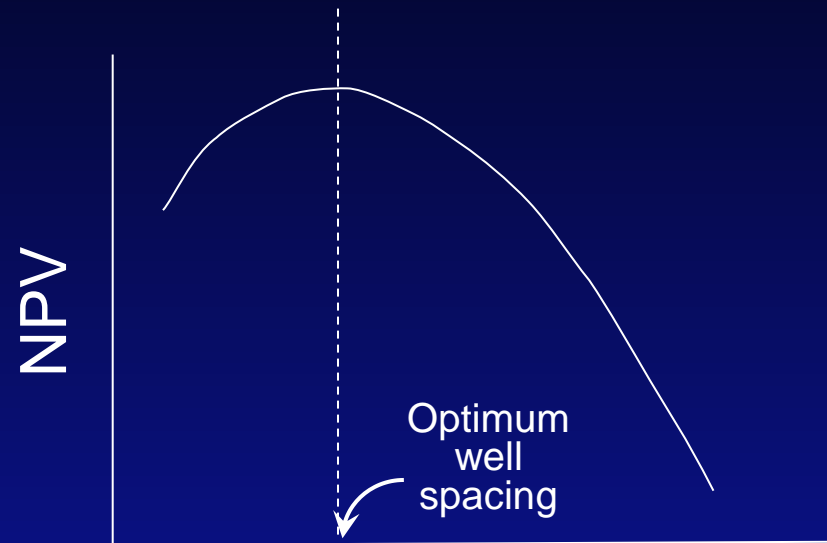


# Conventional Wisdom

## Well Spacing (Drainage Area) for Conventional Plays



Well spacing or  
drainage area

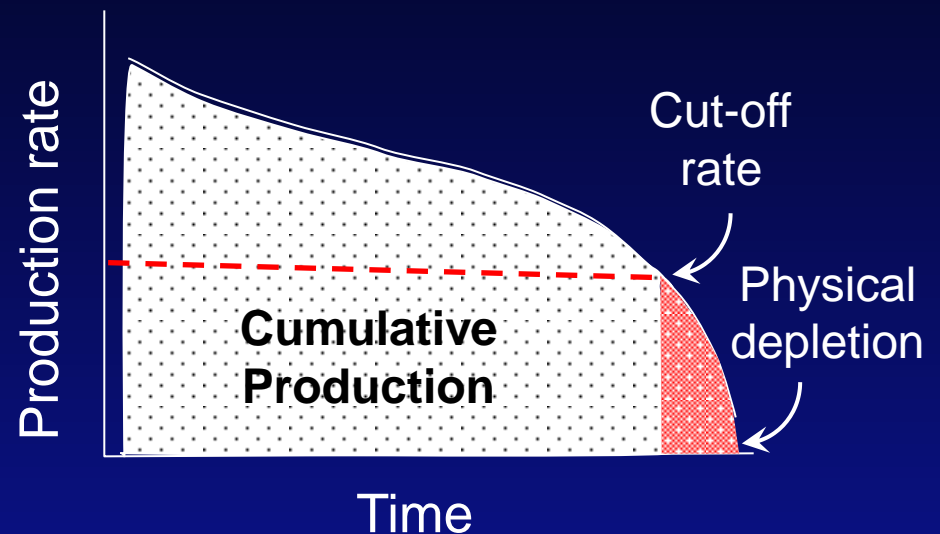
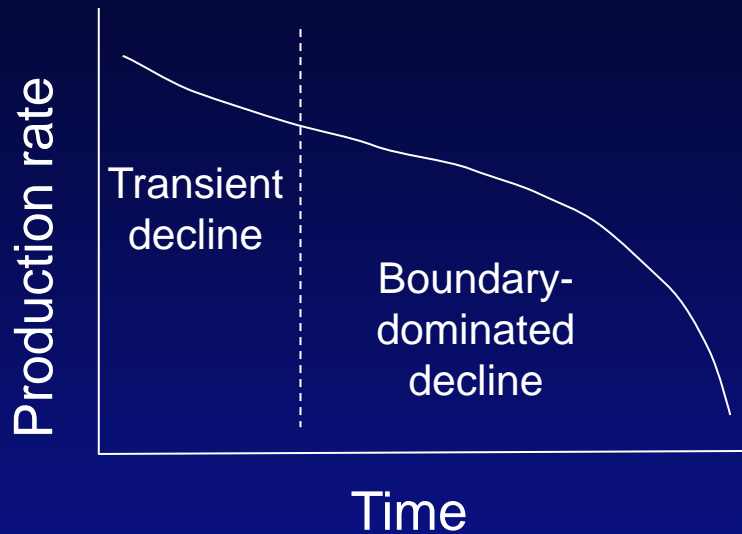


Well spacing or  
drainage area



# Conventional Wisdom

## Well Spacing (Drainage Area) for Conventional Plays



Most conventional wells reach cut-off rate during boundary dominated flow  
At the cut-off rate, the drainage area is close to physical depletion



# Conventional Wisdom

## Well Spacing (Drainage Area) for Conventional Plays

Tighter well spacing accelerates the recovery of reserves, which is favored by project economics

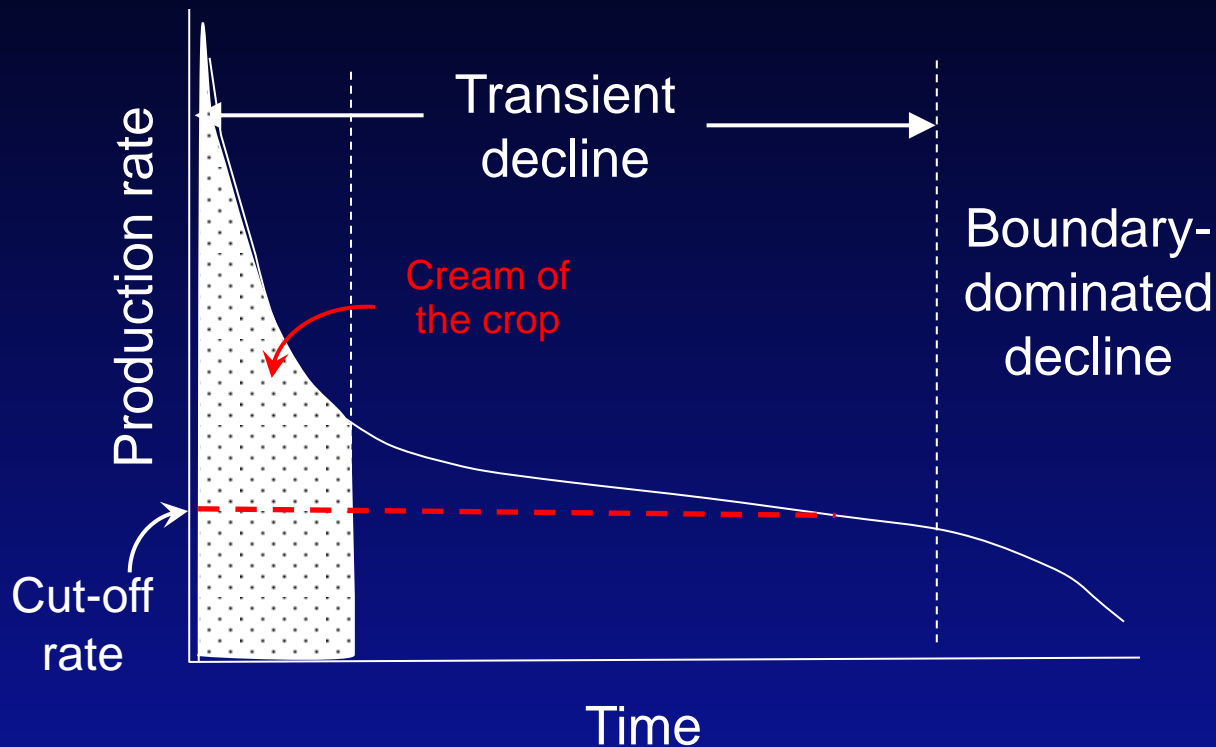
The incremental gain in productivity becomes smaller as the well spacing becomes tighter

For conventional wells, well project economics and well spacing is dictated by physical depletion conditions



# Unconventional Wells

## Production from Unconventional Wells

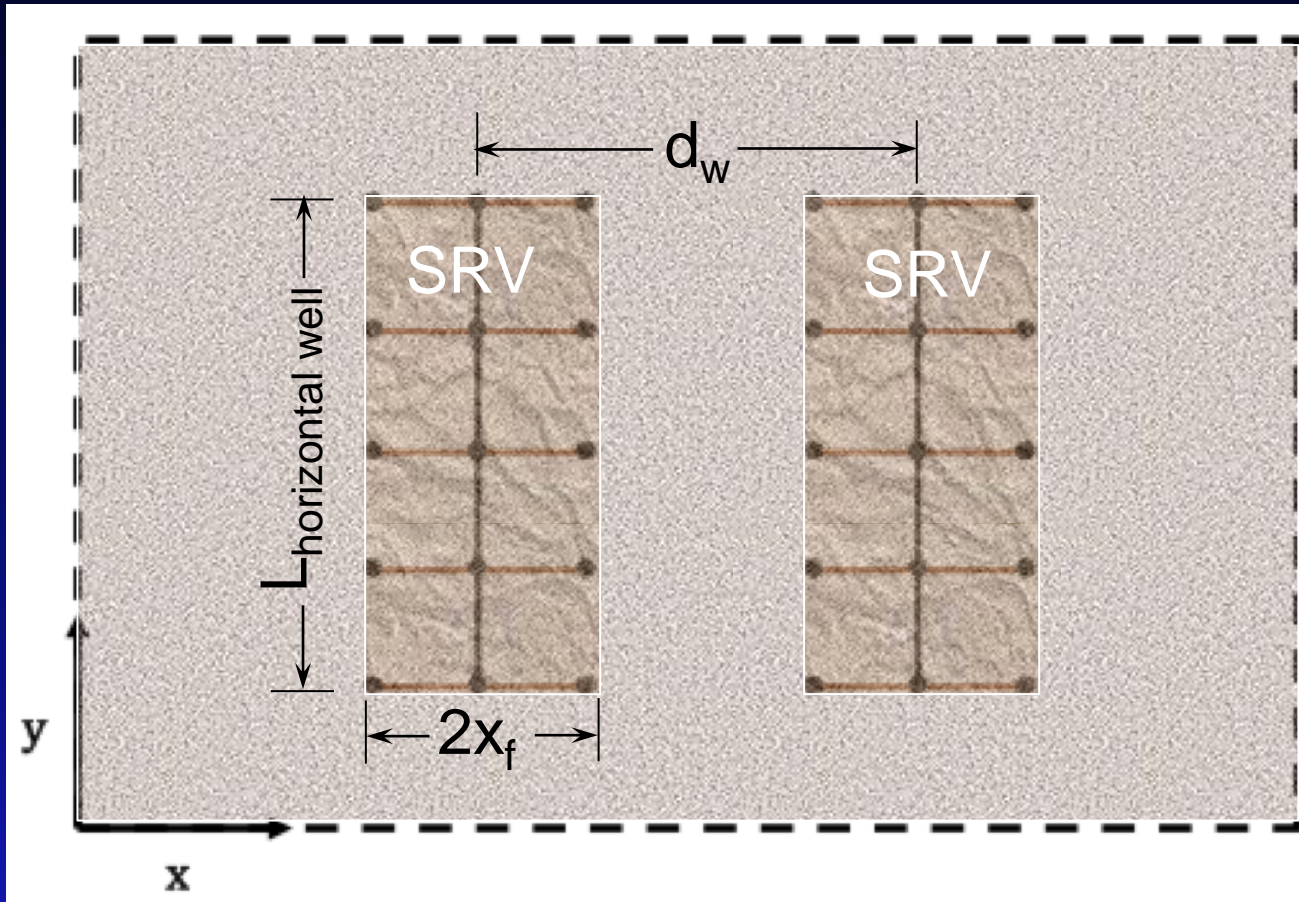


Most unconventional wells reach cut-off rate during transient flow  
Project economics are dictated by economic depletion



# Well Spacing Problem

Well spacing is one of the most important factors affecting the economics of unconventional development projects

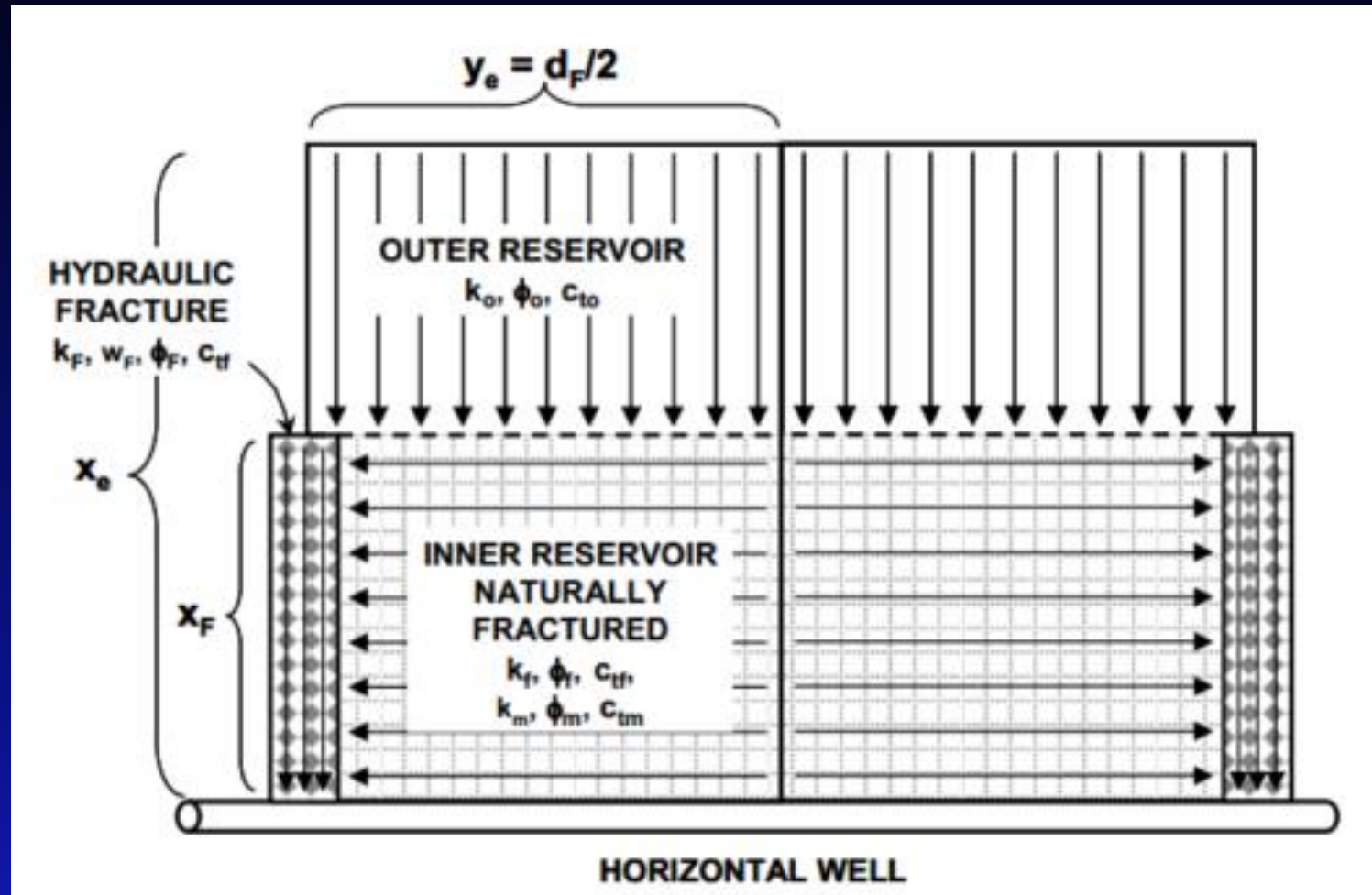


Drainage area of fractured horizontal wells is a function of well spacing and the size of the SRV



# Transient Drainage Area

## Linear flow model





# Transient Drainage Area

## Dimensionless transient linear flow equation

$$P_D = \sqrt{\frac{\pi t_D}{1+\omega}} \exp\left(-\frac{y_D^2(1+\omega)}{4t_D}\right) - \frac{\pi y_D}{2} \operatorname{erfc}\left(\frac{y_D}{2\sqrt{\frac{t_D}{1+\omega}}}\right)$$

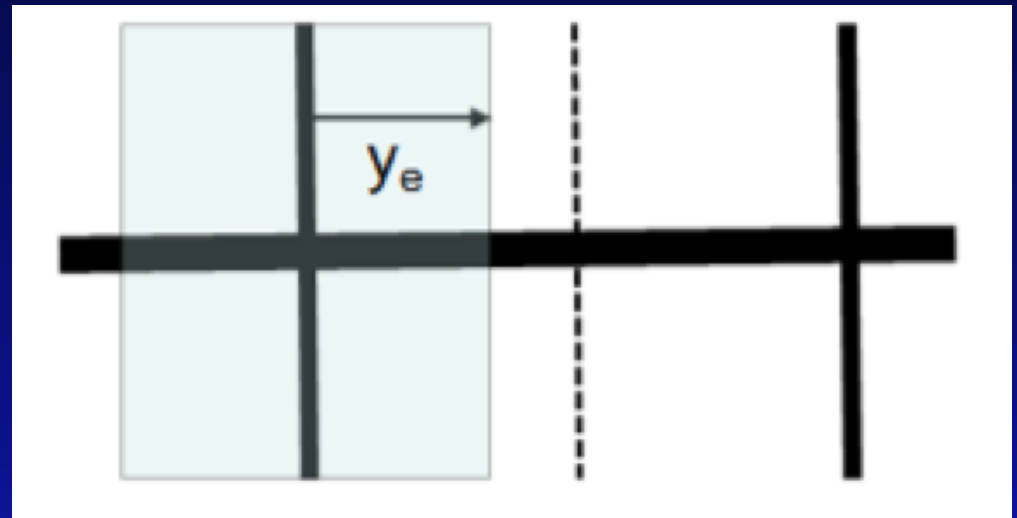
$$P_D = \frac{kh}{141.2qB\mu} (P_i - P)$$

$$t_D = \frac{2.637 \cdot 10^{-4} kt}{fmc_t x_f^2}$$

$$y_D = \frac{y}{x_f}$$

$$\omega = \frac{(\phi c_t)_m h_m}{(\phi c_t)_f h_f}$$

$\omega$  : storativity ratio



# Transient Drainage Area

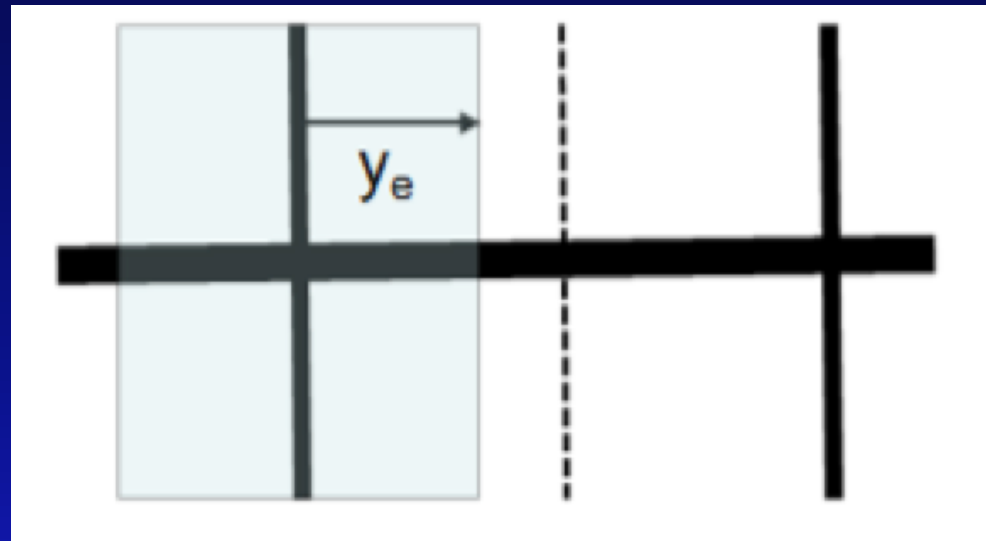
Let  $y_e$  denote the point beyond which the pressure does not change with time

During transient flow,  $y_e = f(t_m)$

The time  $t_m$  is found by differentiating the linear flow solution twice and setting equal to zero

$$t_D = \frac{y_{eD}^2 (1 + \omega)}{2} \quad t_m = \frac{y_e^2 (1 + \omega)}{2\eta}$$

$$y_e = \sqrt{\frac{2\eta t_m}{(1 + \omega)}} \quad h = \frac{2.637 \cdot 10^{-4} k}{f c_t m}$$



# Transient Drainage Area

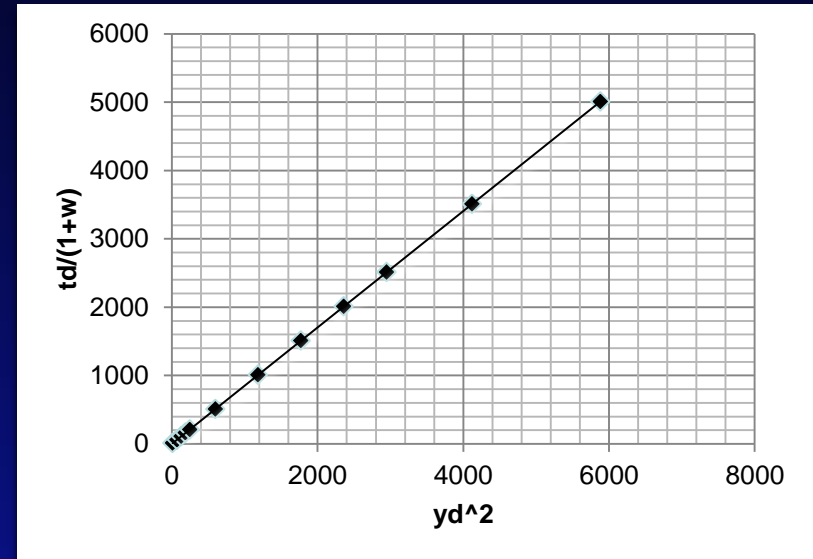
When the pressure from transient linear flow equation becomes equal to the pressure from pseudosteady state linear flow equation:

$$P_{wD} = \frac{2\pi t_D}{1 + \hat{\omega}} + \frac{\pi}{6} \left( y_{eD} - \frac{w_D}{2} \right) + \frac{\pi}{3C_{FD}}$$

$$P_{wD} - \bar{P}_D = \frac{\pi}{6} \left( y_{eD} - \frac{w_D}{2} \right) + \frac{\pi}{3C_{FD}}$$

$$P_D = \sqrt{\frac{\pi t_D}{(1 + \omega)}} \exp\left(-\frac{y_D^2 (1 + \omega)}{4t_D}\right) - \frac{\pi y_D}{2} \operatorname{erfc}\left(\frac{y_D}{2\sqrt{\frac{t_D}{(1 + \omega)}}}\right) = \frac{\pi}{6} y_D$$

$$P_D = \sqrt{\frac{\pi t_D}{(1 + \omega)}} \exp\left(-\frac{y_D^2 (1 + \omega)}{4t_D}\right) - \frac{\pi y_D}{2} \operatorname{erfc}\left(\frac{y_D}{2\sqrt{\frac{t_D}{(1 + \omega)}}}\right) - \frac{\pi}{6} y_D = 0$$



$$t_D = 0.8516 y_D^2 (1 + \omega)$$

$$t_m = \frac{y^2 (1 + \omega)}{1.175\eta}$$



# Transient Drainage Area

$$t_D = 0.5 y_{eD}^2 (1 + \omega)$$

$$t_D = 0.8516 y_D^2 (1 + \omega)$$

$$y_D = 0.77 y_{eD}$$

$y_D$  = Drainage distance

$y_{eD}$  = Distance of investigation

If we substitute  $y_D$  in the transient linear flow equation;

$$P_D = \sqrt{\frac{\pi t_D}{1 + \omega}} \exp\left(-\frac{y_D^2 (1 + \omega)}{4 t_D}\right) - \frac{\pi y_D}{2} \operatorname{erfc}\left(\frac{y_D}{2 \sqrt{\frac{t_D}{1 + \omega}}}\right)$$

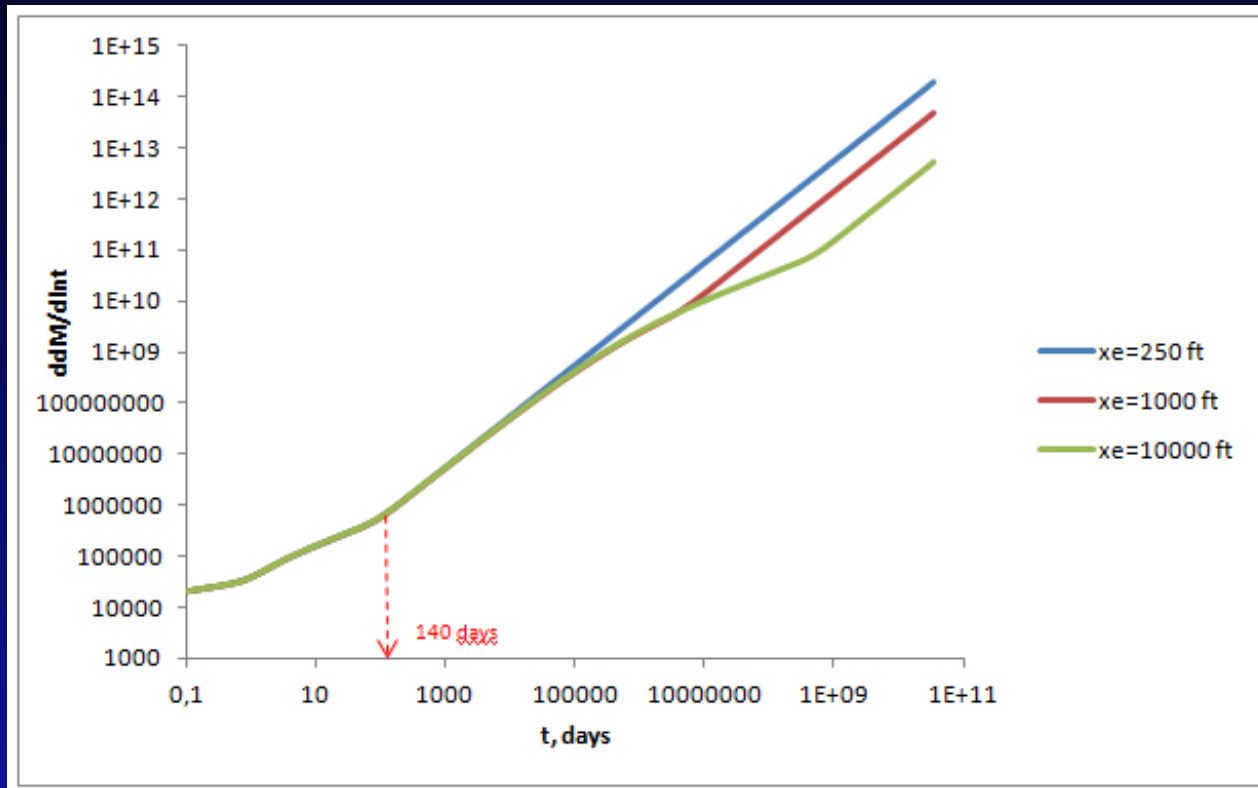
We have

$$P_D = \frac{\pi}{6} y_D$$



# Transient Drainage Area

Example: Reaching physical boundaries

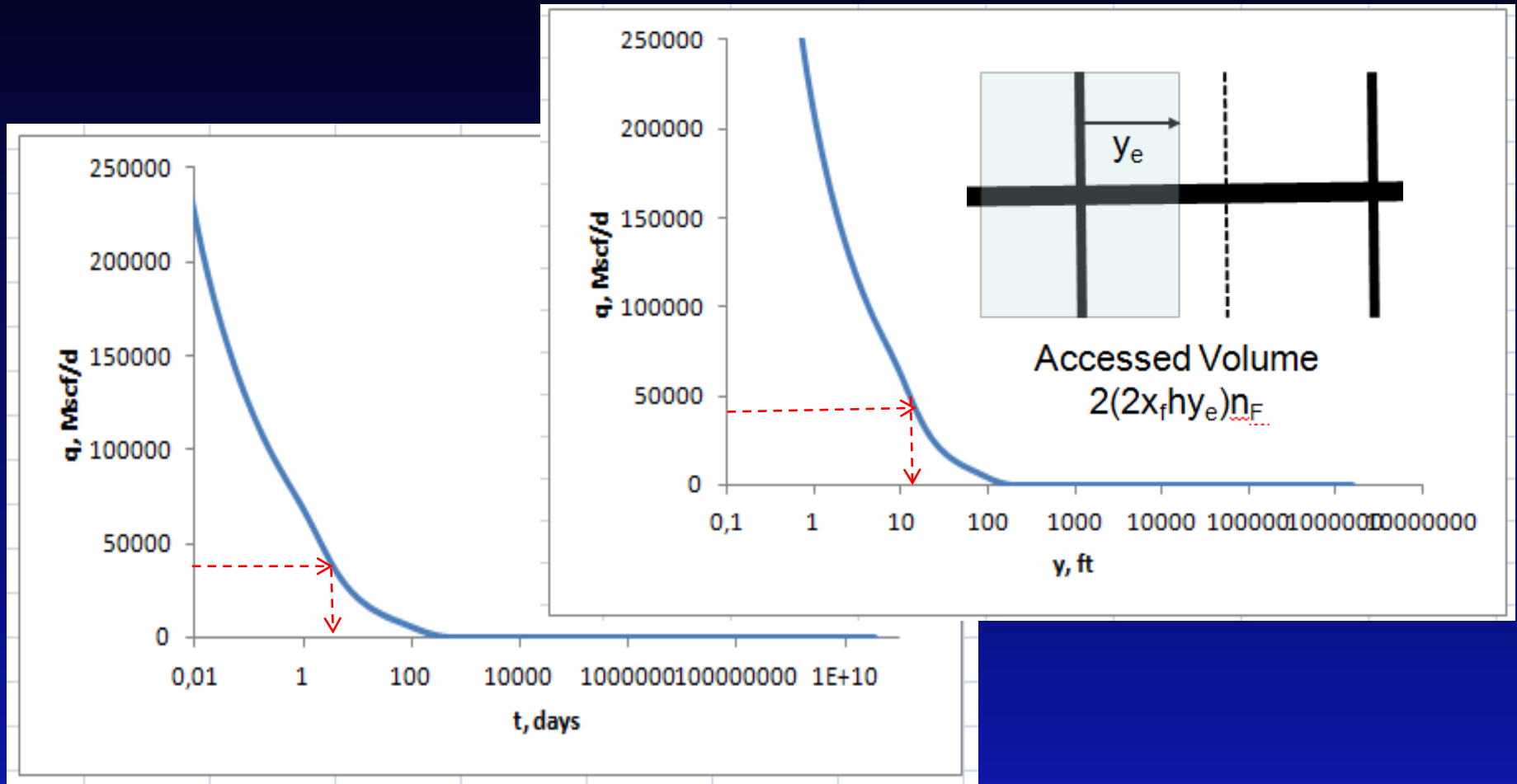


Stabilization Time and the Effect of the Outer Reservoir for the Dual-Porosity Inner Reservoir ( $k_o = 0.0001$  md)



# Transient Drainage Area

## Drainage Volume under Constant Pressure Production



# Transient Drainage Area

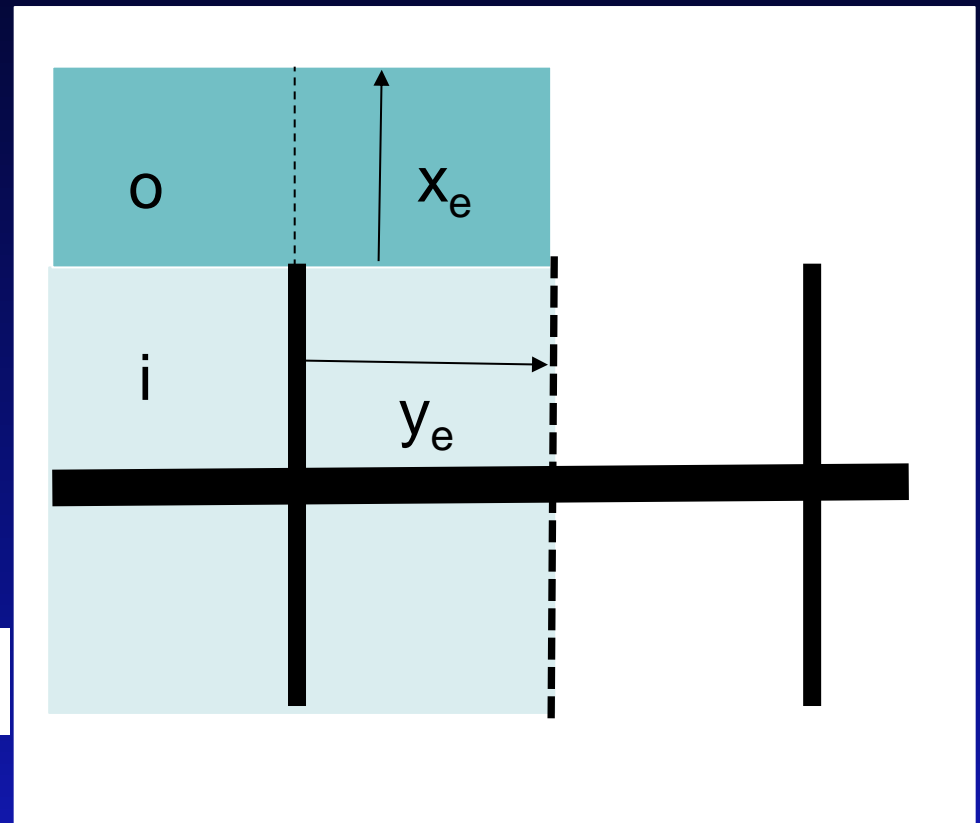
The same approach can be applied to find the accessed reservoir volume beyond SRV

$$t_{om} = \frac{x_e^2}{2h_0} \quad x_e = \sqrt{2\eta_o t_{om}}$$

$$h_0 = \frac{2.637 \cdot 10^{-4} k_o}{(fc_t)_o m}$$

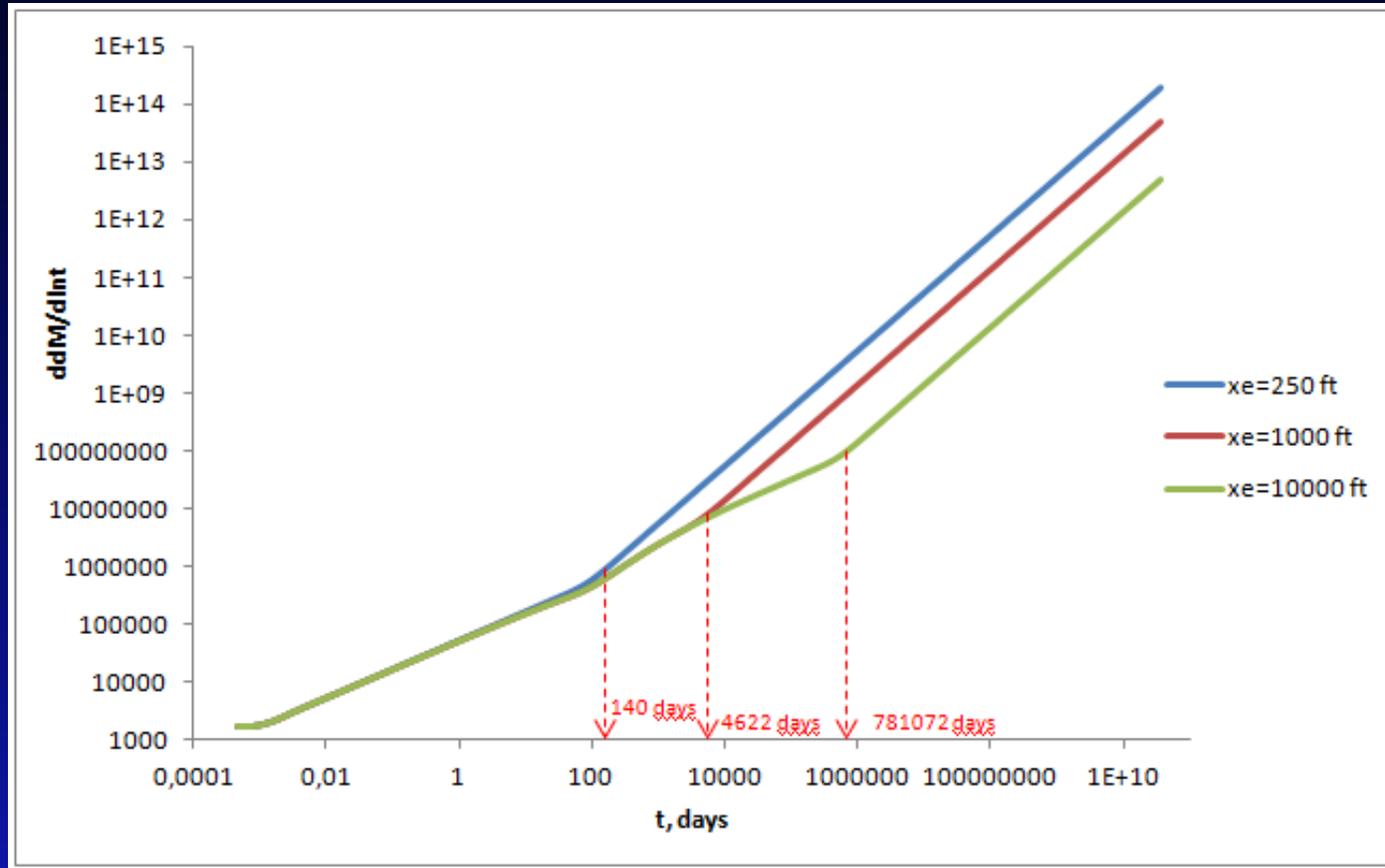
Total Accessed Volume:

$$4(x_f)(h)(y_e)(n_F) + 4(x_e)(y_e)(h)(n_F)$$



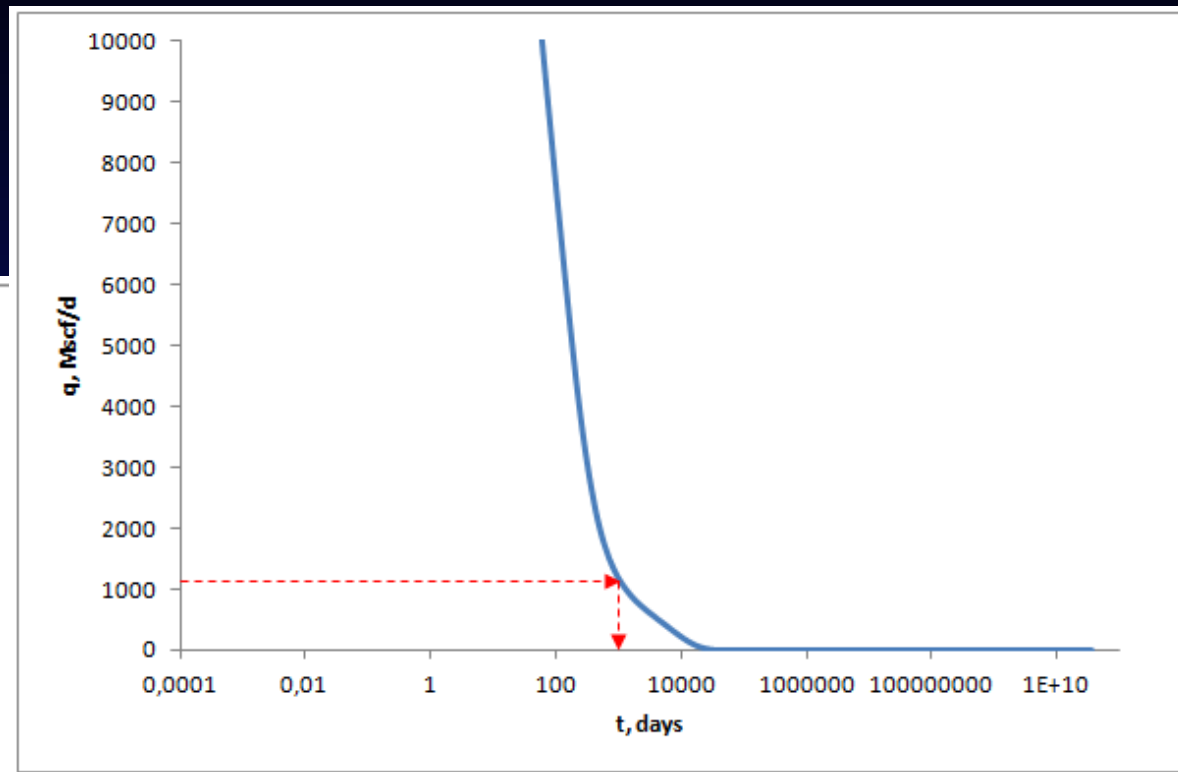
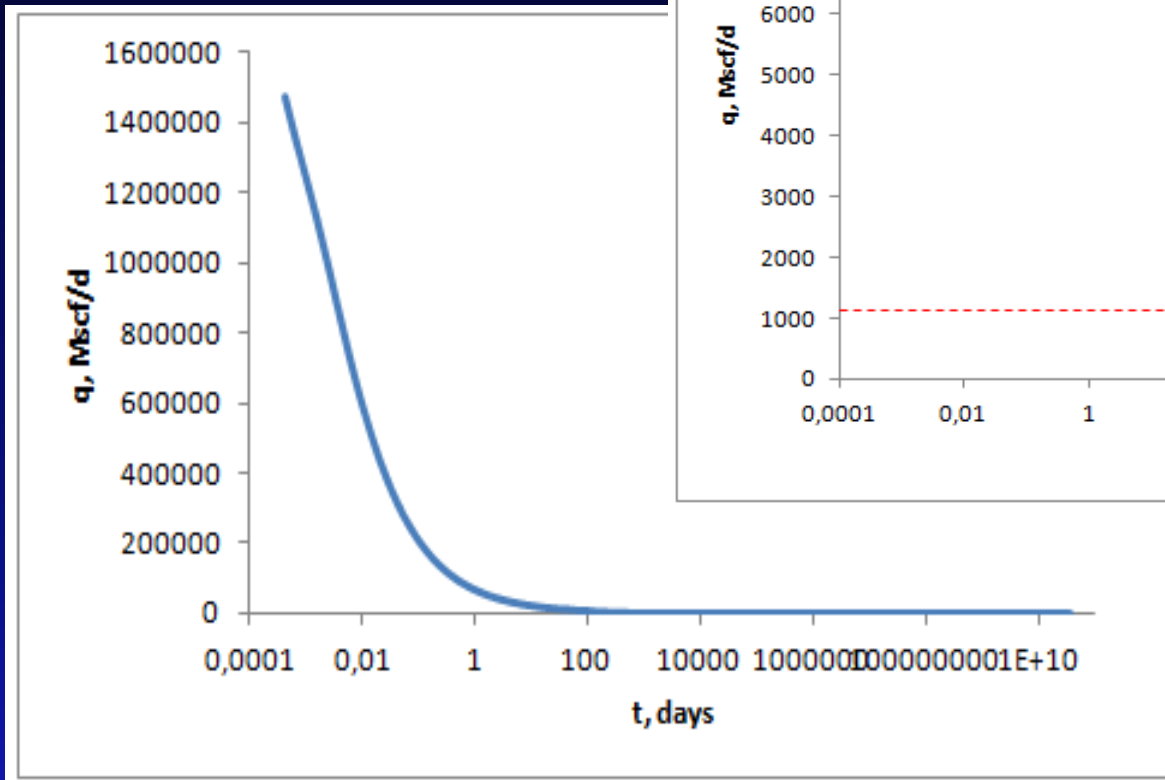
# Transient Drainage Area

Example: Reaching physical boundaries ( $k_0 = 0.1$  md)





# Transient Drainage Area



If we assume an economic cut-off rate of 1200 Mscf/d, we can reach that rate 980 days after the beginning of production.



# Transient Drainage Area

We know that, the flow starts from the outer reservoir 140 days after the beginning of production.

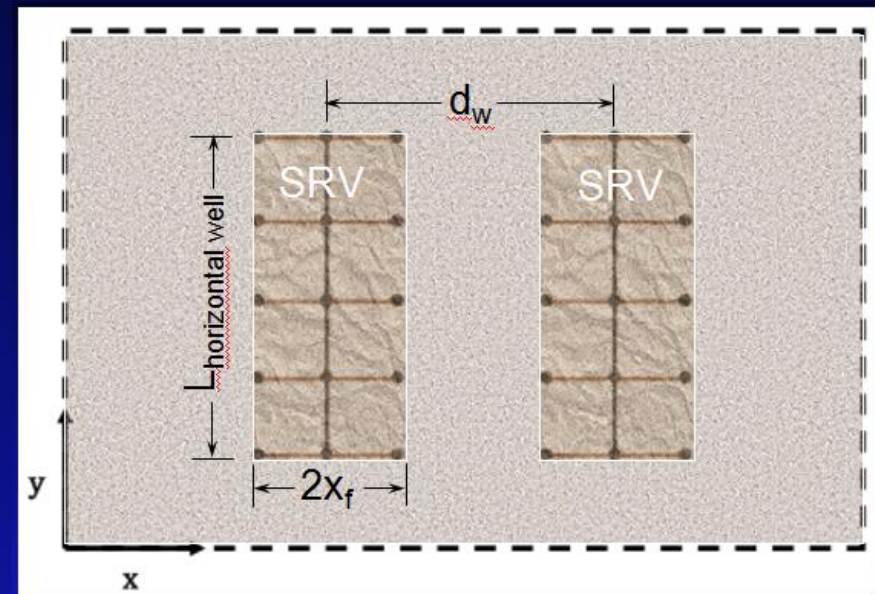
So, there will be flow from the outer reservoir for  $980 - 140 = 840$  days  $\approx$  20160 hours.

Then,

$$y = \sqrt{\frac{5.274 \times 10^{-4} k_m t}{\phi_m \mu_m c_{t_m}}} = \sqrt{\frac{5.274 \times 10^{-4} (0.1)(20160)}{(0.08)(0.013)(0.01)}} = 320 \text{ ft}$$

320 ft of outer reservoir is accessed.

$$d_w = 2(320 + x_f)$$



# Transient Drainage Area

## Accessed Volume Calculation:

→ For Inner Reservoir:

$$4(x_f)(h)(y_e)(n_F) = 4(250)(250)(100)(15) = 375000000 \text{ ft}^3$$

→ For Outer Reservoir:

$$4(x_e)(y_e)(h)(n_F) = 4(320)(100)(250)(15) = 480000000 \text{ ft}^3$$

→ Total:

$$375000000 + 480000000 = 855000000 \text{ ft}^3 = 855 \text{ MMScf}$$



# Conclusions

The drainage area of unconventional wells are dictated by transient decline

Well spacing considerations are not usually related to physical depletion and recovery factors

Using the accessed reservoir volume corresponding to a given economic cut-off rate is a practical approach to optimize well spacing

